

Appendix A: Calculations for Data Quality Assessment (sec. 4-5) aka

What Is Reality?

- 1-pt QC check statistics
- Precision calcs
- Bias calcs

Stats are designed to show us how far from the TRUTH we might be.

- **Measurement Error**

- Presented as a fraction of the “truth” (e.g., 10% off)

- **Precision**

- Random error

- “wiggle” inherent in system

- Estimated by (1) repeated measurements of “known,” and/or (2) side-by-side measurements of the same thing

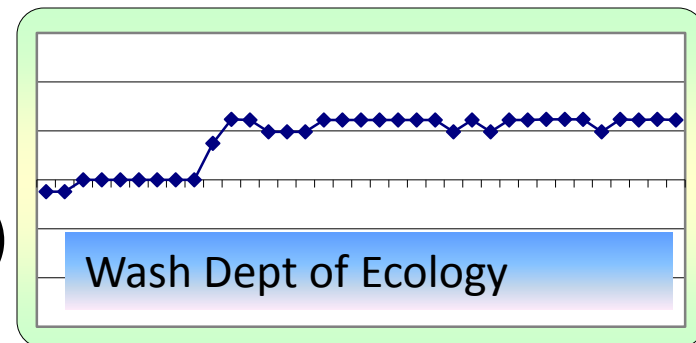
- Some imprecision is unavoidable

- **Bias**

- Systematic error

- “jump” consistently high or low

- bias can be eliminated (in theory)



1-pt QC O₃ check data, in AQS:

SITE 20

Meas Val (Y)	Audit (known) Val (X)
--------------	-----------------------

85.1	91.1
81.6	91.1
83.4	92.4
84	92.4
87.4	92.4
78.4	92.4
85.4	92.4
85.4	92.4
80.6	88
83.5	88
83.5	88
80.8	88
81.5	88
93.5	88
84.8	88

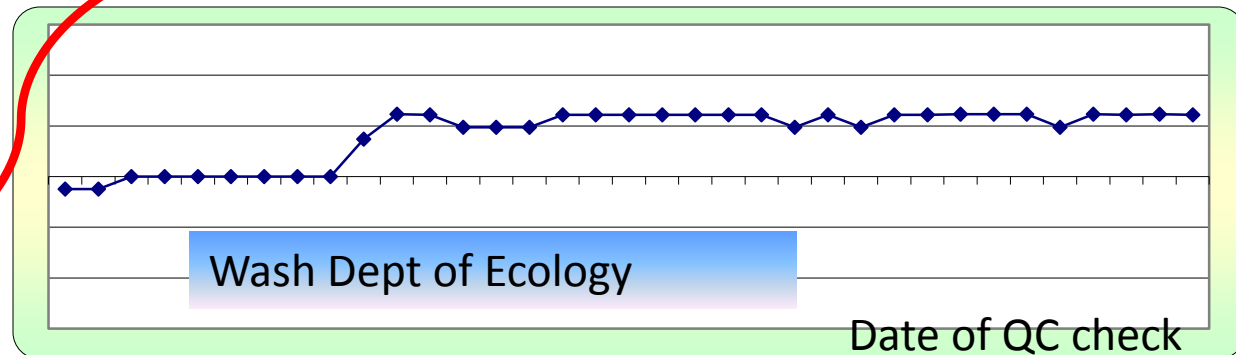


$$d\text{-sub-}i = d_i = \text{diff}/\text{known}$$

- Routine QC checks used to estimate BOTH
- Both come from **d-sub-i**

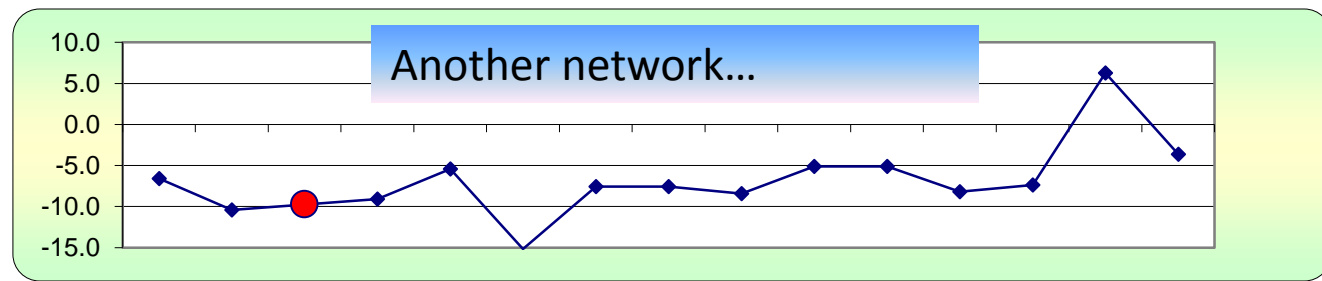
- Bias

- Precision



- sometimes it's obvious

- Sometimes it's not:

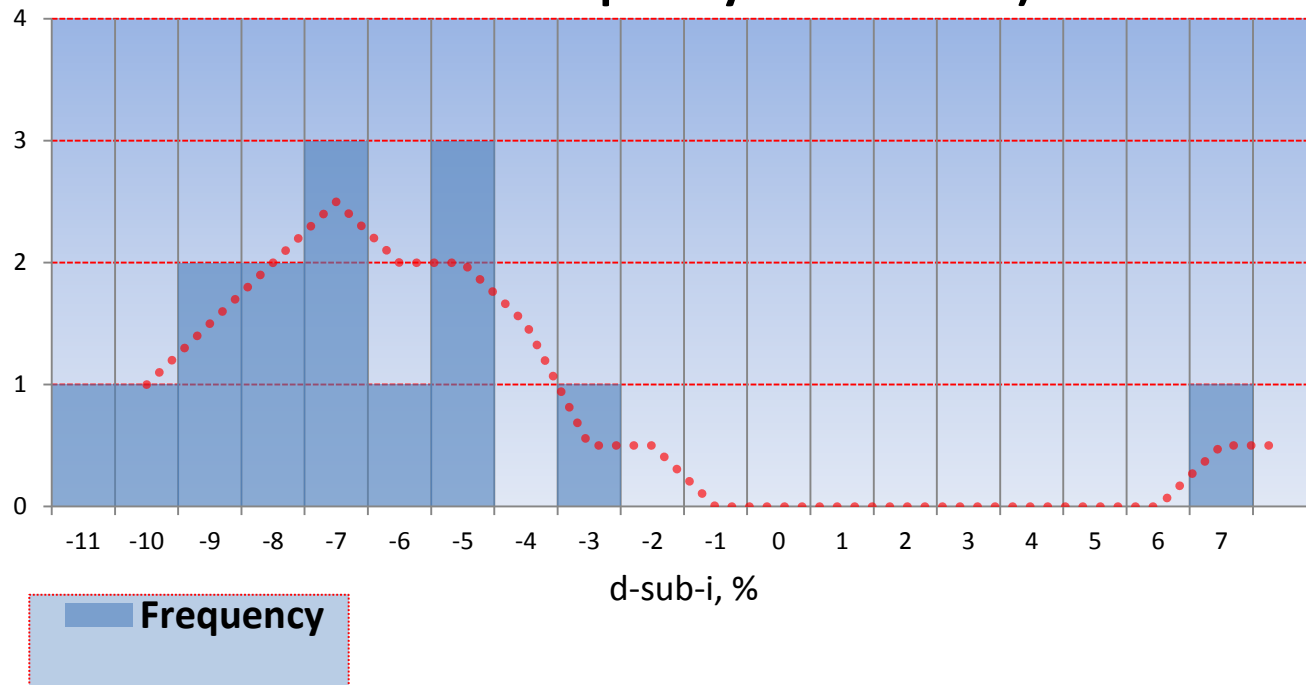


Meas Val (Y)	Audit Val (X)	d-sub-i
85.1	91.1	-7
81.6	91.1	-10
83.4	92.4	-10
84	92.4	-9
87.4	92.4	-5
78.4	92.4	-15
85.4	92.4	-8
85.4	92.4	-8
80.6	88	-8
83.5	88	-5
83.5	88	-5
80.8	88	-8
81.5	88	-7
93.5	88	6
84.8	88	-4

- d-sub-i values represent:
 - All of the measurements' error during that day, week, month, quarter
 - The QC checks are supposed to be “randomized” so that they are a sample, or subset, of the whole universe of possible QC checks (the population), and then represent the population of QC checks you could do at any time
 - As a proportion of the “truth,” so “**truth**” is always on the bottom (diff/known; so error is quantified as a fraction of the truth so we can imagine it, e.g., 10%)
 - “error” = distance from truth at that moment

Meas Val (Y)	Audit Val (X)	d-sub-i
85.1	91.1	-7
81.6	91.1	-10
83.4	92.4	-10
84	92.4	-9
87.4	92.4	-5
78.4	92.4	-15
85.4	92.4	-8
85.4	92.4	-8
80.6	88	-8
83.5	88	-5
83.5	88	-5
80.8	88	-8
81.5	88	-7
93.5	88	6
84.8	88	-4

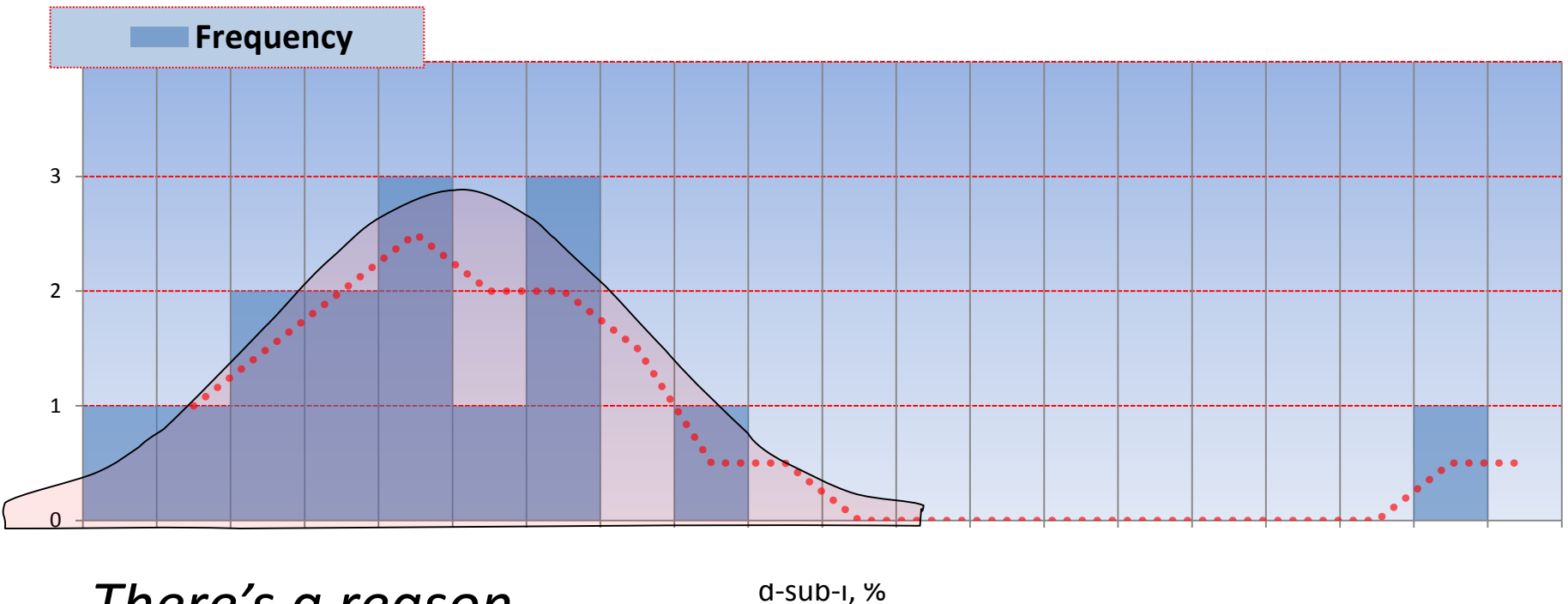
O3 one-point QC checks: d-sub-i histogram (aka frequency distribution)



*How can we apply these results to get **bias** and **precision** for ALL our measurements of ozone with this analyzer during this time period?*

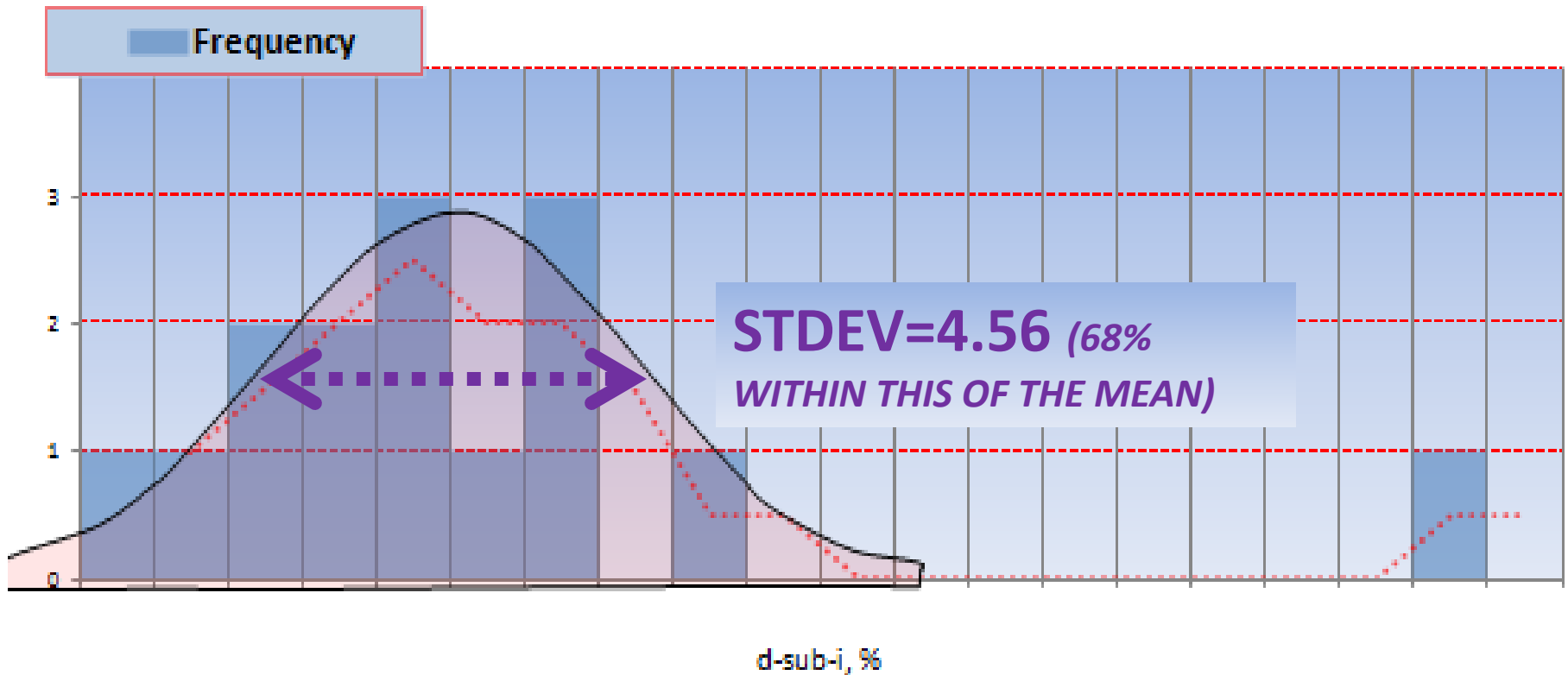
We assume that these results, and their distribution, is representative of all the QC checks we could have done:

O3 one-point checks: d-sub-i histogram (aka frequency distribution)

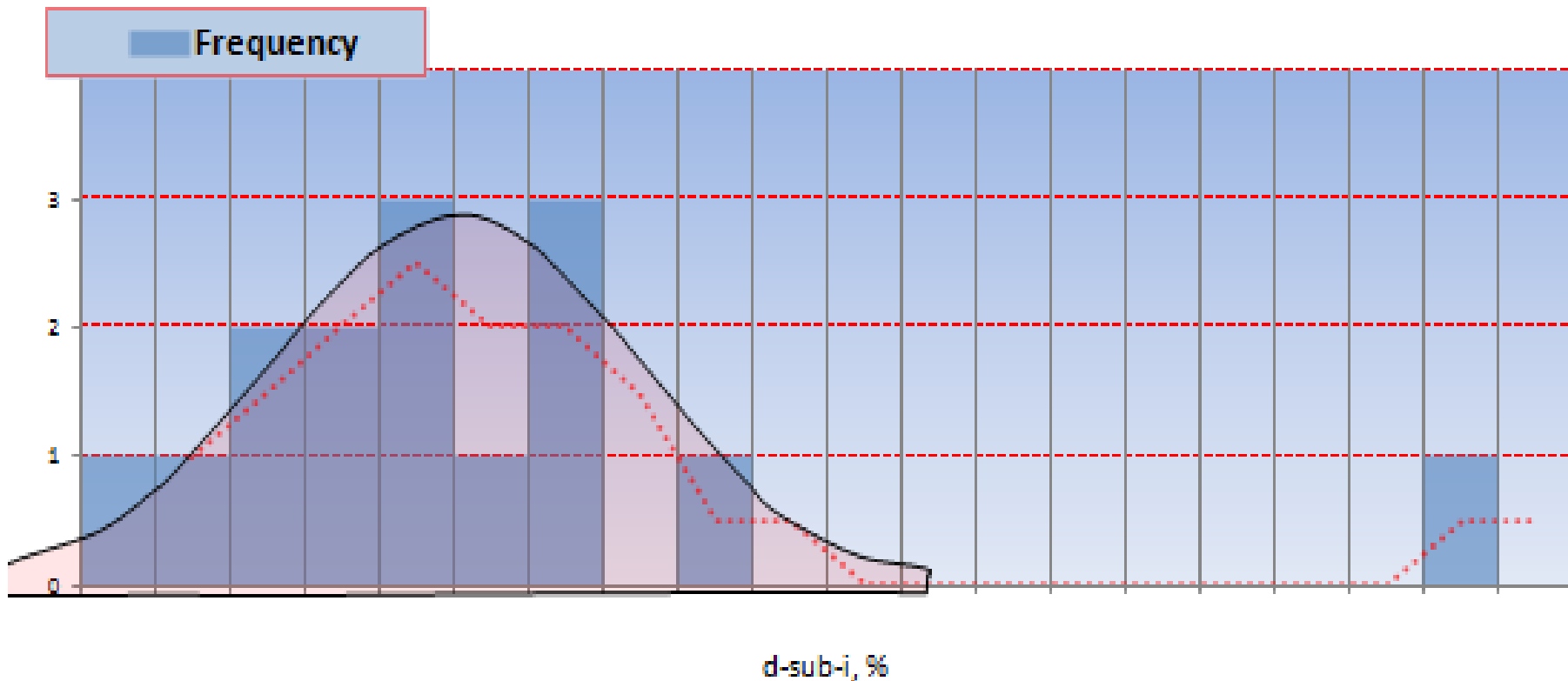


*There's a reason
no x-axis units*

The goal for acceptable measurement uncertainty is defined for O3 precision as an upper 90 percent confidence limit for the coefficient variation (CV) of 7%



- But we do not care about the low-imprecision tail
- Only care about the extreme tail of high imprecision
- Want to be able to say “90% confident that your precision is less than this value”

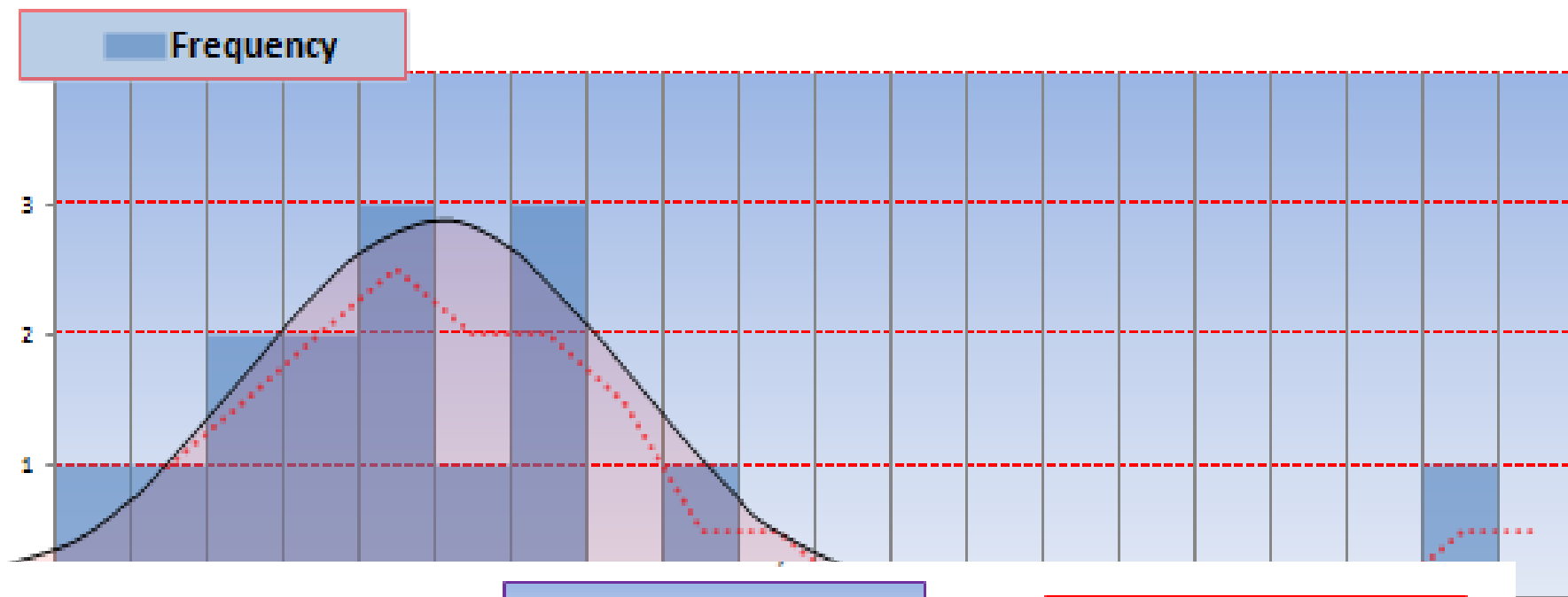


STDEV=4.56

10% upper tail

CFR
eq'n
2:

$$\text{Precision_Estimate} = \sqrt{\frac{n \cdot \sum_{i=1}^n d_i^2 - (\sum_{i=1}^n d_i)^2}{n(n-1)}} \cdot \sqrt{\frac{n-1}{\chi_{0.1, n-1}^2}}$$



STDEV=4.56

10% upper tail

$$\text{Precision_Estimate} = \sqrt{\frac{n \cdot \sum_{i=1}^n d_i^2 - (\sum_{i=1}^n d_i)^2}{n(n-1)}} \cdot \sqrt{\frac{n-1}{\chi_{0.1, n-1}^2}}$$

chi-sqrd(90%) = CHIINV(0.9,n) = 7.79

then $4.56 \times \text{SQRT}(n-1/7.79) = 6.11 \%$

Use the DASC Tool to Understand Your QC Checks and Audit Results (like EPA does)

- Calculations of measurement uncertainty are carried out by EPA, *and* PQAOs should report the data for all measurement quality checks
- YOU do these calculations and charts easily, and save yourself time, money, and embarrassment



We will review each in both the DASC tool and the AMP256 report

First, what is the DASC tool?

- ▶ DASC tool was produced specifically for us to calculate the data assessment statistics in CFR in AMTIC Quality Indicator Assessment Reports (AMP256)
- ▶ <http://www.epa.gov/ttn/amtic/qareport.html>
- ▶ Easy way to explain and calculate data assessment statistics in CFR
- ▶ Excel spreadsheet
- ▶ Matches AMP256 (by site)
- ▶ Each equation is numbered and matches the numbers in CFR

O₃ Assessments

[Print Worksheet](#)

Precision in DASC = cell i13 = 6.11%

O₃ Assessments

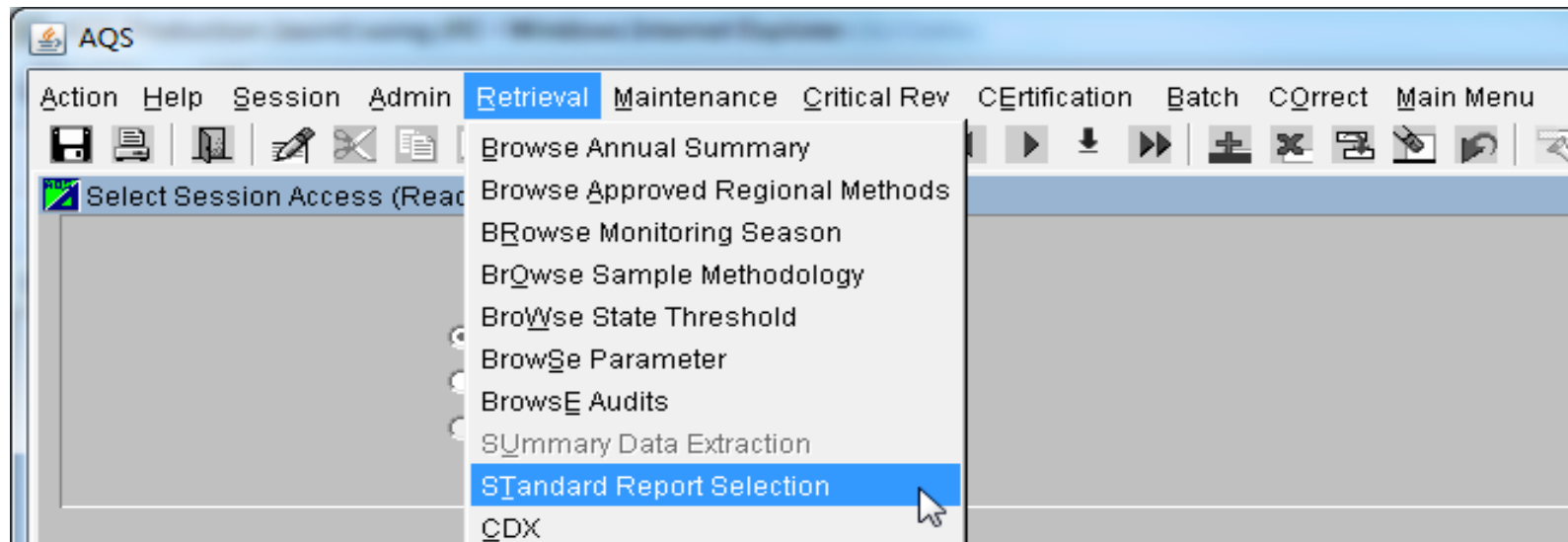
site 20		Pollutant type: O ₃	
Meas Val (Y)	Audit Val (X)	d (Eqn. 1)	
85.1	91.1	-6.586	
81.6	91.1	-10.428	
83.4	92.4	-9.740	
84	92.4	-9.091	
87.4	92.4	-5.411	
78.4	92.4	-15.152	
85.4	92.4	-7.576	
85.4	92.4	-7.576	
80.6	88	-8.409	
83.5	88	-5.114	
83.5	88	-5.114	
80.8	88	-8.182	
81.5	88		
93.5	88		
84.8	88		

CV (%) (Eqn 2)
6.11

$$Precision_Estimate = \sqrt{\frac{n \cdot \sum_{i=1}^n d_i^2 - (\sum_{i=1}^n d_i)^2}{n(n-1)}} \cdot \sqrt{\frac{n-1}{\chi_{0.1, n-1}^2}}$$

AMP256-Data Quality Indicators Report

- AQS Standard Report to Compute the Statistics Outlined on 40 CFR Part 58 Appendix A
- Part of the Annual Certification Process to Verify Submission of QA and routine Data to AQS



- **CORRESPONDS to what you can calculate in the DASC spreadsheet, as we will see.**

Does our **6.1%** match AMP256?

DATA QUALITY INDICATOR REPORT

One Point Quality Control

Jun. 16, 2014

PQAO: Virginia I

App A? Y

POC	MT	Begin Date	End Date	# Required	# Observation	% Complete	CV UB	Bias UB
1	S	01-APR-12	31-OCT-12	15	15	100	6.11	- 8.98

- 90% Confidence Upper Bound of precision is **6.1%**
- “There is a 90% chance that our precision will not be greater than 6.1%”
- Same as YOU can calculate any time using the DASC

Summary of precision:

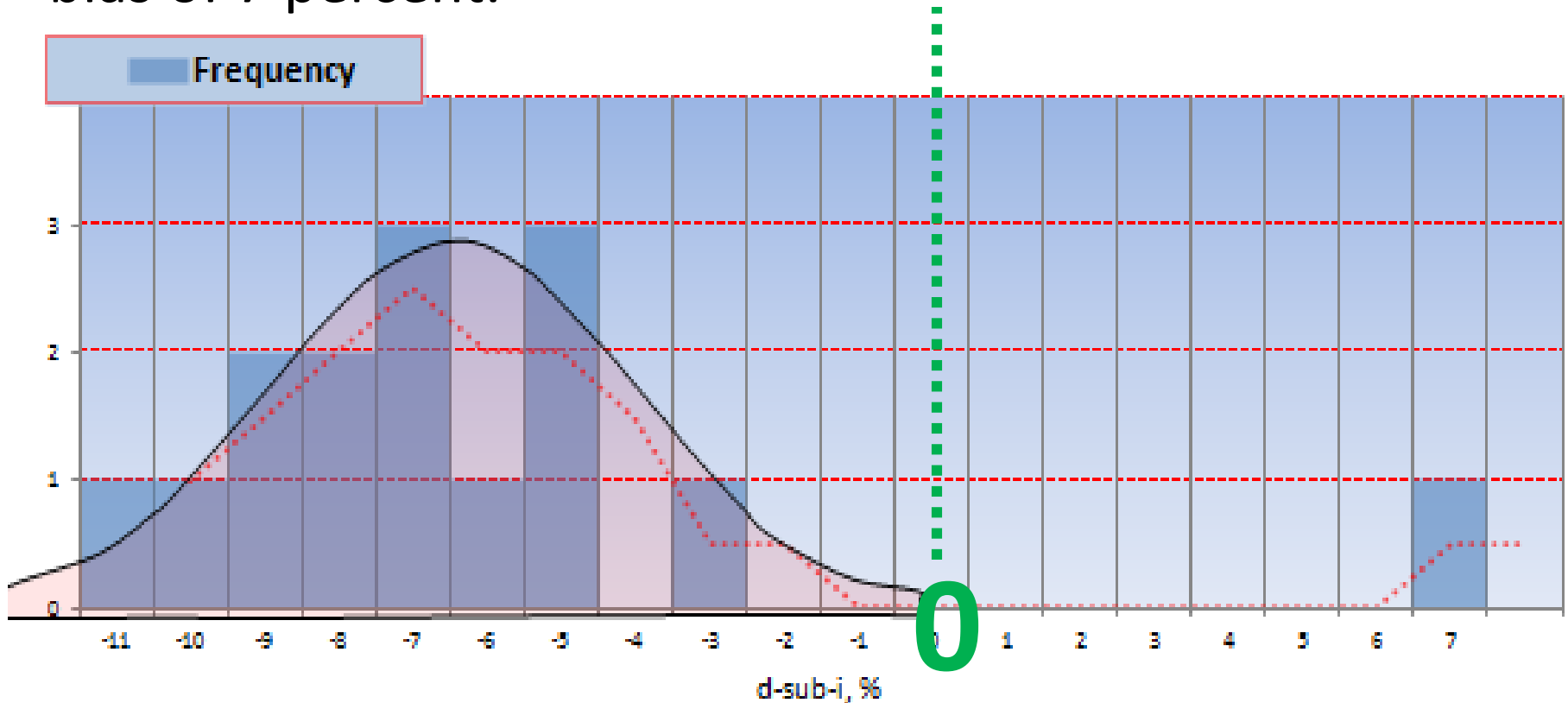
- Calculated from routine QC checks d_i
- Overall upper bound of CV calculated from d_i
- you can be **90% sure that your true precision is less than** this “upper bound of the CV” (eq’n 2)



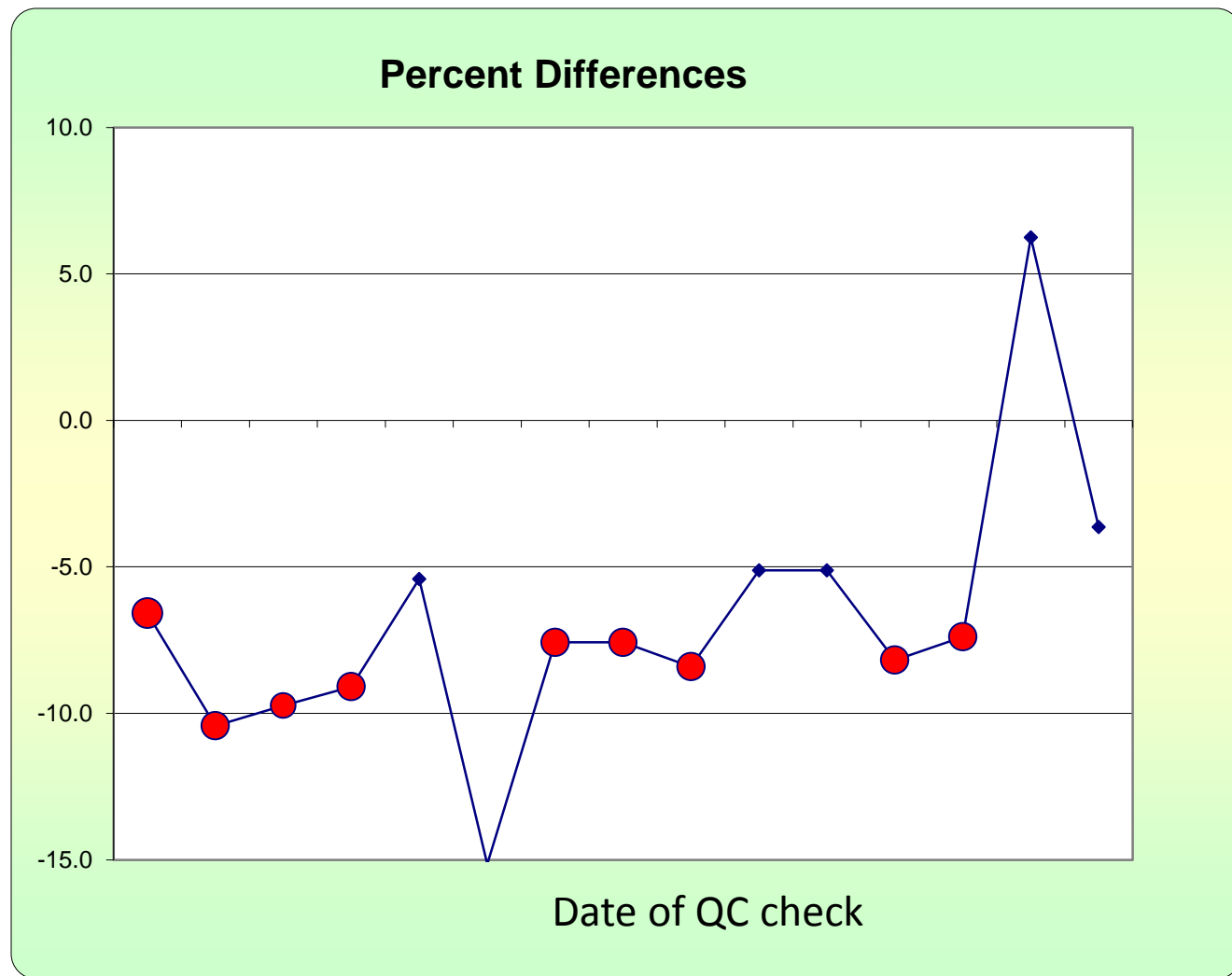
Thanks Shelly
Eberly!

Bias:

- FINALLY look at where we are on the x-axis
- (Remember precision only cares about width)
- The goal for acceptable measurement uncertainty for bias is an upper 95 percent confidence limit for the absolute bias of 7 percent.



Meas Val (Y)	Audit Val (X)	d % (Eqn. 1)
85.1	91.1	-7
81.6	91.1	-10
83.4	92.4	-10
84	92.4	-9
87.4	92.4	-5
78.4	92.4	-15
85.4	92.4	-8
85.4	92.4	-8
80.6	88	-8
83.5	88	-5
83.5	88	-5
80.8	88	-8
81.5	88	-7
93.5	88	6
84.8	88	-4



Control chart from the free DASC
excel spreadsheet on AMTIC

Bias statistics (CFR App A, 4.1.3):

- Remember that bias as well as precision starts from the difference between your instrument's indicated value and the known (audit) value $(\text{meas} - \text{known}) / \text{known} = d_i$
- bias (jump) is calculated from d_i
- Bias just *based on* the AVERAGE of the d_i with the sign taken into account (if your analyzer is always higher than the known, you have a high (+) bias)

Bias in CFR eq'n 3:

$$|bias| = AB + t_{0.95, n-1} \cdot \frac{AS}{\sqrt{n}}$$

AB is the mean of the absolute values of the d_i 's = **7.7**

$t_{0.95, n-1}$ is the 95th quantile of a t -distribution
= $TINV(2*0.05, n-1) = 1.76$

AS is the STDEV of the abs value of these d_i 's = **2.78**

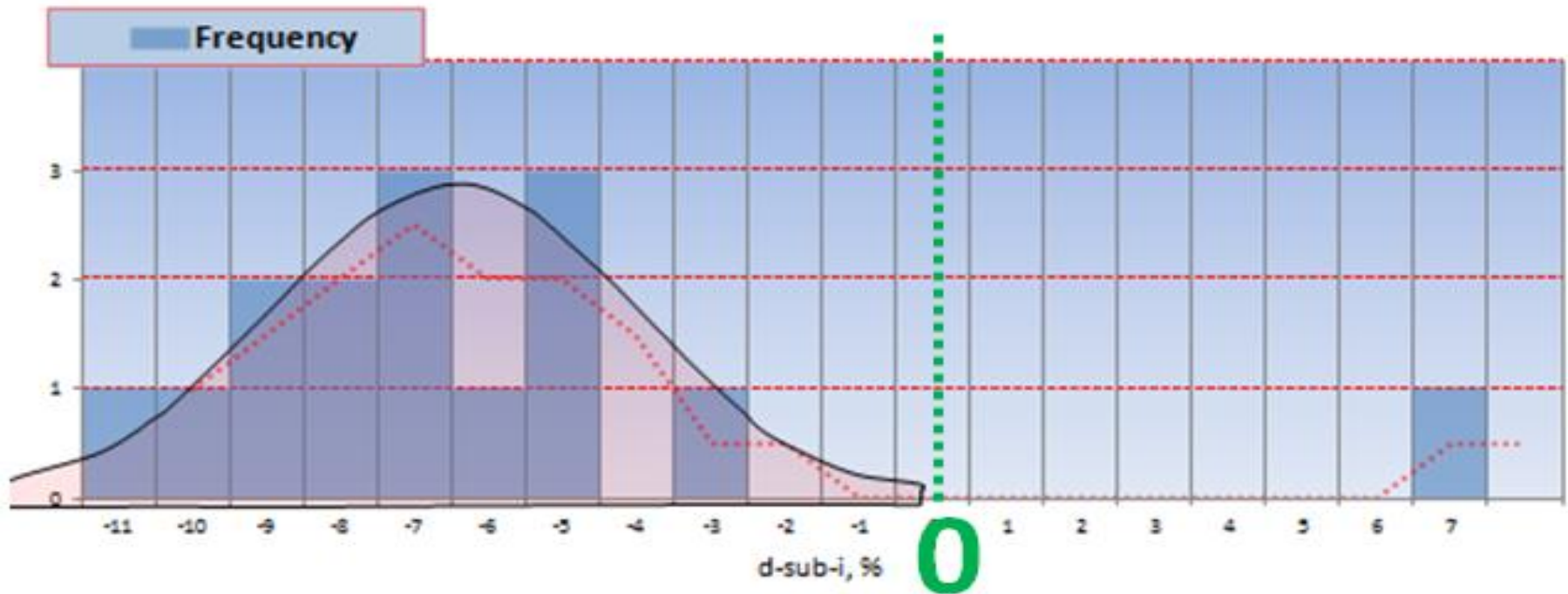
So

Abs value of bias = **7.7** + 1.76 * (**2.78**/sqrt of n)

= **8.98**

d % (Eqn. 1)
-7
-10
-10
-9
-5
-15
-8
-8
-8
-5
-5
-8
-7
6
-4

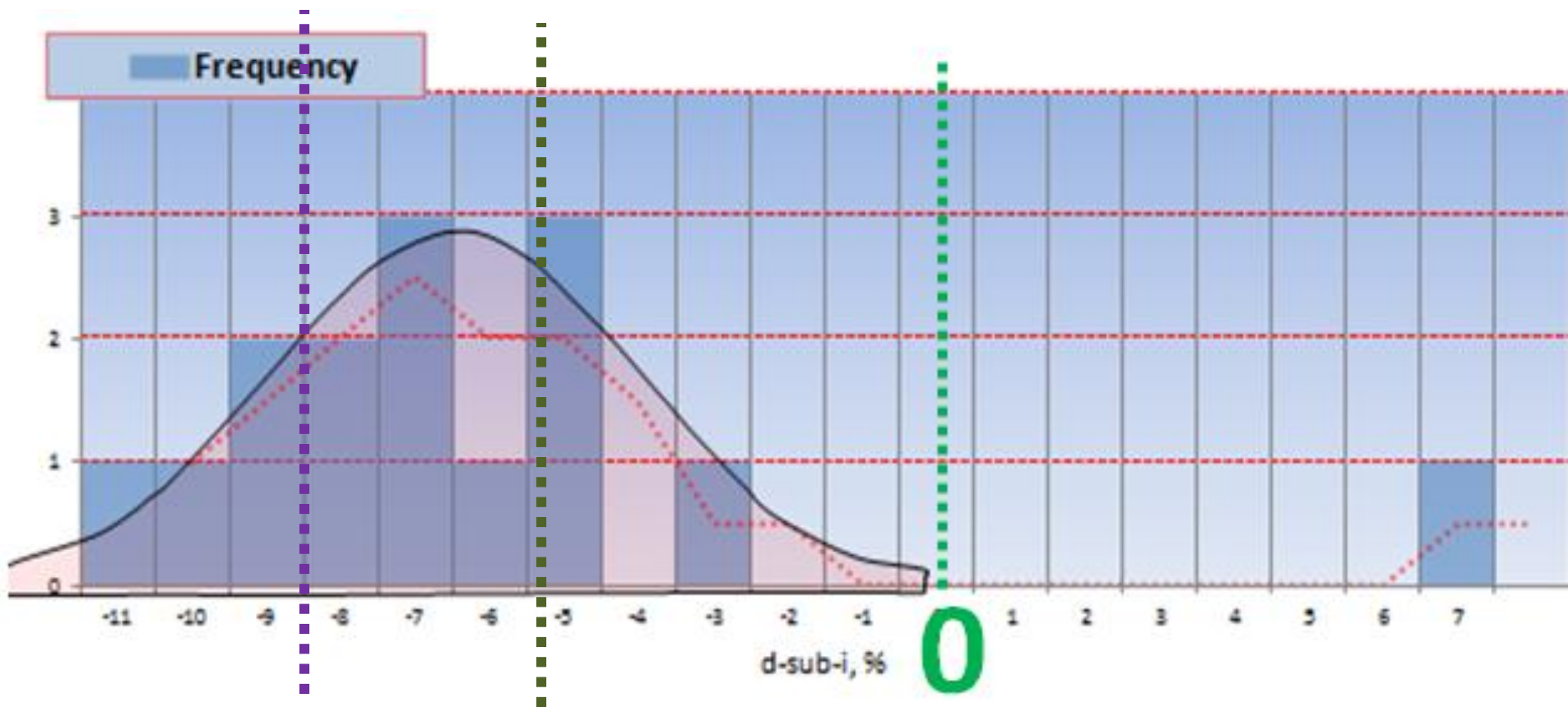
That 8.98 is the abs value of bias, now what's its sign?



- Look at 25% quartile and 75% quartile
- If they straddle zero, bias is unsigned
- If they're both negative, bias is negative
- If they're both positive, bias is positive

Quartiles?

- $\text{=QUARTILE(d-sub-i,1)} = 25\% \text{ quartile} = -9$
- $\text{=QUARTILE(d-sub-i,3)} = 75\% \text{ quartile} = -5$



Sign of Bias:

- Both quartiles are negative
- Bias is negative 8.98 = **-8.98**
- Agrees with DASC:

O ₃ Assessments					CV _{ub} (%)		Bias (%)	
Pollutant type: O ₃								
d (Eqn. 1)	25th Percentile	d ²	d	d ²				
-6.586	-8.750	43.378	6.586	43.378				
-10.428	75th Percentile	108.745	10.428	108.745	n	S _d	S _{d2}	Σ d
-9.740	-5.262	94.873	9.740	94.873	15	4.557	52.464	115.651
-9.091		82.645	9.091	82.645	n-1	Σd	Σd ²	Σ d ²
-5.411		29.282	5.411	29.282	14	-103.151	1000.072	1000.072
-15.152		229.568	15.152	229.568				
-7.576		57.392	7.576	57.392			Bias (%) (Eqn 3)	Both Signs Positive
-7.576		57.392	7.576	57.392			8.98	FALSE
-8.409		70.713	8.409	70.713	CV (%) (Eqn 2)		Signed Bias (%)	Both Signs Negative
-5.114		26.149	5.114	26.149	6.11		-8.98	TRUE
-5.114		26.149	5.114	26.149				
-8.182		66.942	8.182	66.942	Upper Probability Limit		Lower Probability Limit	
-7.386		54.558	7.386	54.558	2.06		-15.81	
6.250		39.063	6.250	39.063				
-3.636		13.223	3.636	13.223				

DASC bias in cell k13:

O ₃ Assessments									
20		Pollutant type: O ₃			Bias (%)				
as	Val	lit	Val	(Eqn. 1)	25th Percentile				
85.1	91.1			-6.586	-8.750				
81.6	91.1			-10.428	75th Percentile				
83.4	92.4			-9.740	-5.262	<div><div>"AB" (Eqn 4) 7.710</div><div>"AS" (Eqn 5) 2.783</div></div> <div><div>Bias (%) (Eqn 3) 8.98</div><div>Signed Bias (%) -8.98</div></div> <div>Both Signs Positive FALSE</div> <div>Both Signs Negative TRUE</div>			
84	92.4			-9.091					
87.4	92.4			-5.411					
78.4	92.4			-15.152					
85.4	92.4			-7.576					
85.4	92.4			-7.576					
80.6	88			-8.409					
83.5	88			-5.114					
83.5	88			-5.114					
80.8	88			-8.182					

Does this match AQS standard report AMP256 ?:

DATA QUALITY INDICATOR REPORT

One Point Quality Control

Jun. 16, 2014

PQAO: |

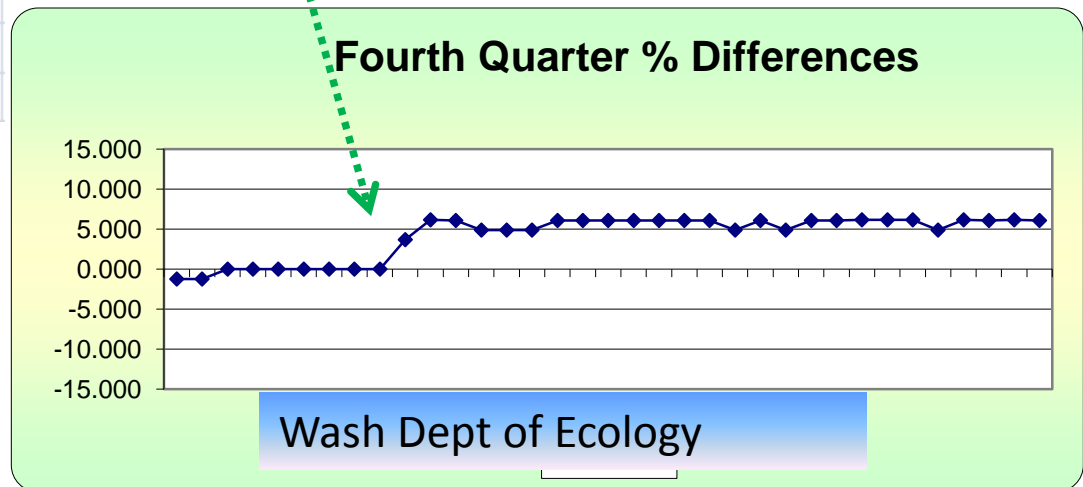
POC	MT	Begin Date	End Date	# Required	# Observation	% Complete	CV UB	App A? Y	Bias UB
1	S	01-APR-12	31-OCT-12	15	15	100	6.11		- 8.98

Bias UB (*upper bound of bias*) = -8.98
(*goal is upper 95 percent confidence limit for the absolute bias of 7 percent*)

Both bias and precision are in the same sheet (O3 P&B) in the DASC and use the same input:

Meas Val (Y)	Audit Val (X)	d_i (Eqn. 1)
0.08	0.081	-1.2
0.08	0.081	-1.2
0.081	0.081	0.0
0.081	0.081	0.0
0.081	0.081	0.0
0.081	0.081	0.0
0.081	0.081	0.0
0.081	0.081	0.0
0.081	0.081	0.0
0.084	0.081	3.7
0.086	0.081	6.2
0.087	0.082	6.1

YOU can calculate Bias over any time period using DASC



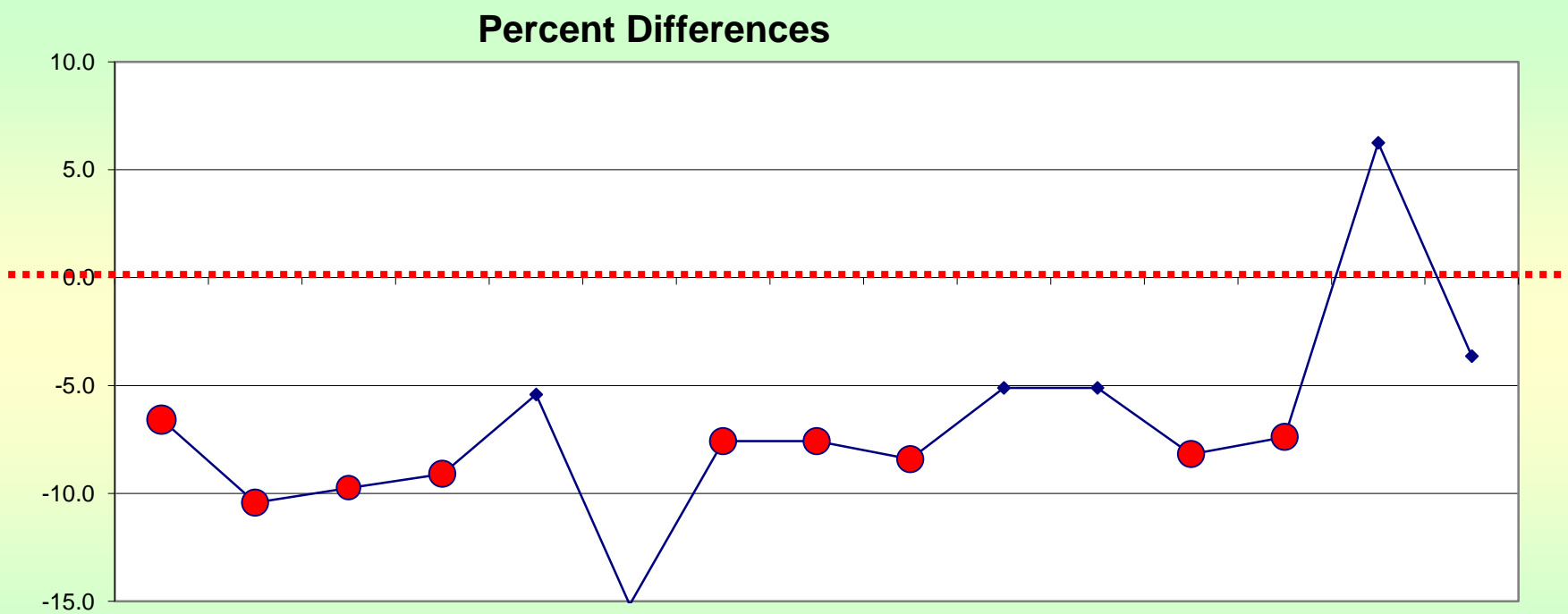
Summary of gas **bias**:

- Calculated from routine QC checks **d_i**
- Overall upper limit of **bias** calculated from **d_i**
- Then look at the sign (and the chart) for whether your analyzer is biased high (+) or low (-)
- We are 95% confident that our 03 bias is less extreme than -9%

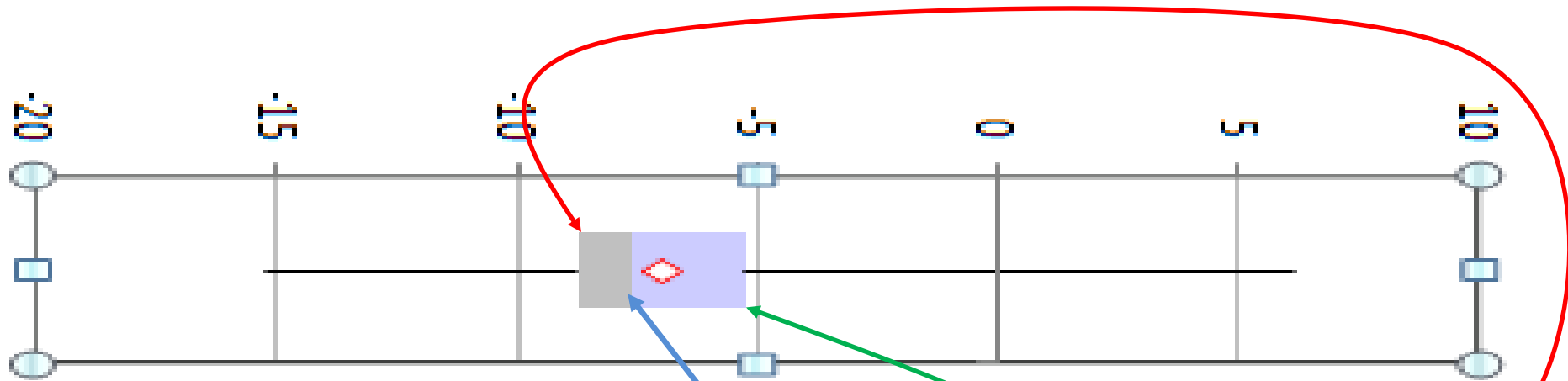
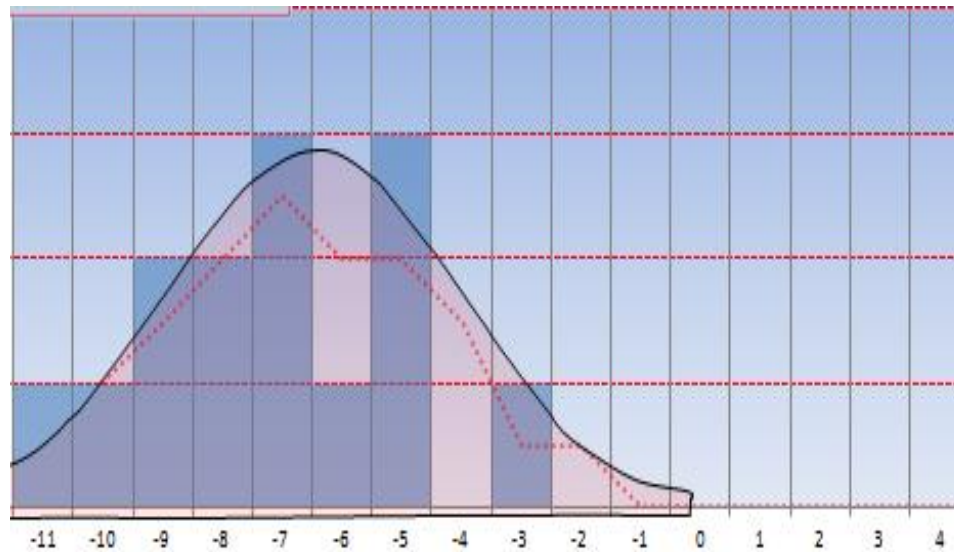


Do I invalidate pollutant data based on d-sub-i?

- Validation tables in QA Handbook:
 - Critical Measurement Quality Objective O3=7%
 - See the Data Certification ppt, next up.




Date of QC check



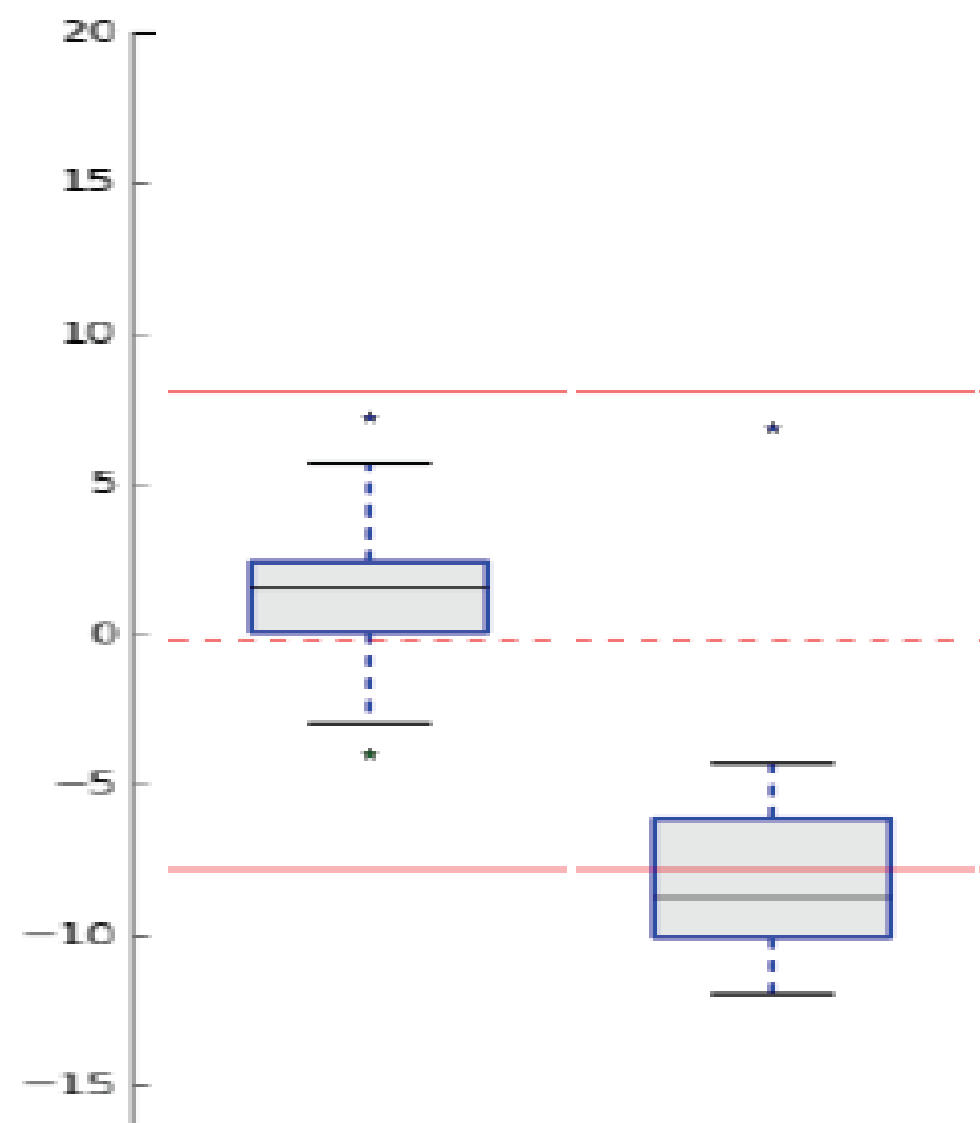
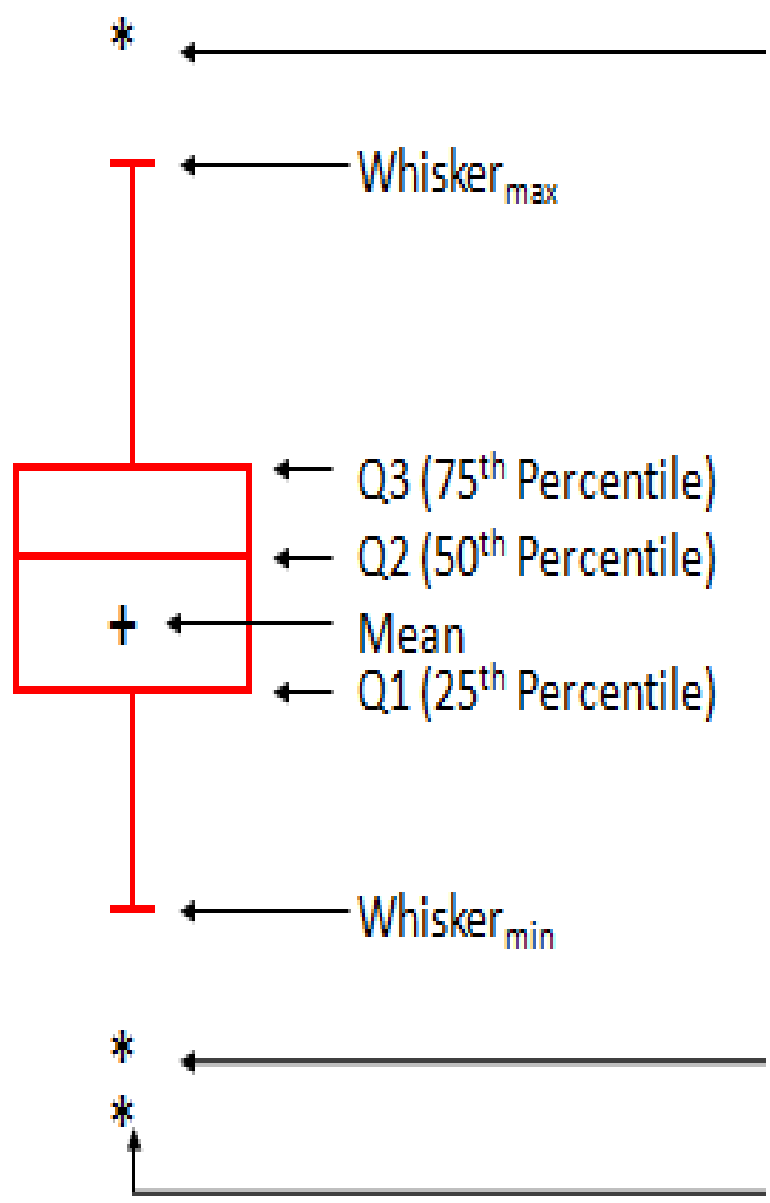
Median = 50% percentile = -7.6

25% percentile = -8.8

75% percentile = -5.3

Mean = -6.9 

	CV	2.56	6.11
	Bias	+2.44	-8.98
	# Obs	31	15
	Method	047	047



PM_{2.5} Precision

- PM2.5 is the same as gaseous, except:
 - d-sub-i are from COLLOCATED, and the known is the average of the two PM2.5, so d-sub-i is
 - (RO-CO)/(avg of RO & CO)
 - Because the known is the avg of 2 measurements, add **SQRT(2)** to the denominator (divide by best estimate of truth)

$$CV_{ub} = \sqrt{\frac{n \cdot \sum_{i=1}^n d_i^2 - \left(\sum_{i=1}^n d_i \right)^2}{2n(n-1)}} \cdot \sqrt{\frac{n-1}{\chi_{0.1, n-1}^2}}$$

STDEV

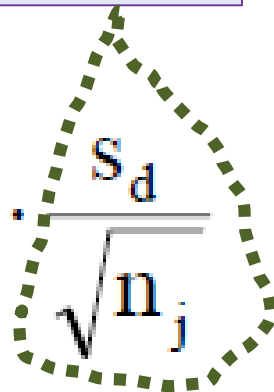
That's the only difference in the precision stat from gas stats

PM_{2.5} Bias

- PM_{2.5} bias same as gaseous, except:
 - known = PEP audit filter results, so the d-sub-i is the (field-PEP)/PEP
 - Don't take abs value of the d-sub-i
 - D is avg of these d-sub-i values
 - n is # of PEP audits, and if n=3 then t=2.9
 - (as n grows, t goes to 1.65)
 - Use the 25% and 75% quartiles ➡ + or -

Stnd
error

$$\text{Upper 90\% Confidence Interval} = D + t_{0.95, df} \cdot \frac{s_d}{\sqrt{n_j}}$$



And lower confidence interval
is D minus t*stnd error

PM10 statistics:

- Bias confidence intervals based on monthly flow rate (FR) checks:
 - d-sub-i from FR
 - THEN bias statistics are the same as PM2.5
- Flow rate “acceptability” limits are based on 6-month FR audits (with FR audit device not the same one you use for the monthly):
 - Limit = $D \pm 1.96 * STDEV$

d-sub-i = (sampler-audit_FR)/audit_FR
and D is their average

Thank you!

- Work with Tribal Air Agencies
- Knowledge = Power; Let's Share
- Melinda Ronca-Battista melinda.ronca-battista@nau.edu; this presentation is on our YouTube channel

